A Fast Algorithm for Computing Doppler Introduced by Sea Surface Gravity Waves

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1 Introduction and History

- 2 Basic Mathematics for Modeling Time-Varying Environments
- Operational Algorithms for Modeling Time-Varying Environments
- Applications to Acoustic Communications
- **5** Summary and Conclusions

Introduction

Motivation for our work

- Acoustic modem performance is more than just transmission loss!
- Computationally efficient algorithms for the rigorous modeling of the effects of the sound channel on a given timeseries were needed

- The VirTEX algorithm was developed to address the issues introduced by time-varying environments, and utilizes post-processing of the output from contemporary ray tracing computer programs
- Our efforts have produced two new (more efficient) algorithms;
 - VirTEX for Platform Motion (VirTEX Extra-Lite)
 - VirTEX for Sea Surface Motion (VirTEX Lite)

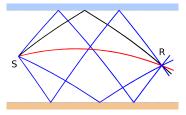
- VirTEX (Virtual Timeseries EXperiment) algorithm
 - See M. Siderius, M. Porter, JASA, vol. 124, no. 1, pp. 137-150
 - Based on post-processing of *multiple* ray tracing computations
 - Suitable for modeling of arbitrary forms of environmental motion
 - The most demanding of computational resources

• VirTEX for Platform Motion (VirTEX Extra-Lite) algorithm (New!)

- Based on post-processing of a *single* ray tracing computation
- Capable of modeling only steady source and receiver motion
- The least demanding of computational resources
- VirTEX for Sea Surface Motion (VirTEX Lite) algorithm (New!)
 - Based on post-processing of a single ray tracing computation
 - Capable of modeling unsteady sea surface, source and receiver motion
 - Some restrictions on the sea surface motion

Basic Mathematics for Modeling Time-Varying Environments Ray Tracing in Static and Time-Varying Environments

• Ray tracing methods compute N eigenrays or paths from src to rcv



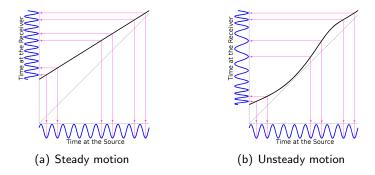
- Each path has an associated amplitude A_i and arrival or travel time τ_i
- The receiver timeseries is given by the convolution of the source timeseries *s*(*t*) with the impulse response of the channel

$$r(t) = \sum_{i=1}^{N} A_i s(t - \tau_i)$$

• For time-varying environments, A_i and τ_i become functions of time

Basic Mathematics for Modeling Time-Varying Environments Computing the Receiver Timeseries Associated with an Eigenray

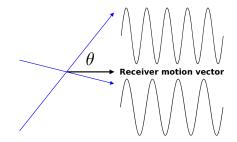
• The receiver timeseries (for a given eigenray) is found by evaluating the *inverse* of the "wall clock" arrival time $f(t) = t + \tau(t)$



- For steady motion, this reduces to the familiar result
 - Receiver timeseries is a time stretch and shift: $r(t) = s(t_0 + \frac{t-t_0-\tau_0}{1+(\frac{\nu}{2})})$
 - Chirp Z transform can compute r(t) efficiently for $t_0 = \tau_0 = 0$

Practical Algorithms for Modeling Time-Varying Environments The VirTEX for Platform Motion (VirTEX Extra-Lite) Algorithm

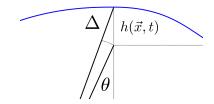
- Algorithm supports only steady source and/or receiver motion
- Path dependent stretching factor becomes $1 + (\frac{v_r}{c})\cos(\theta)$



- "Library" of pre-stretched waveforms (using Chirp Z transform)
- Compute convolution as before, but using pre-stretched waveforms
- The least demanding of computational resources

Practical Algorithms for Modeling Time-Varying Environments The VirTEX for Sea Surface Motion (VirTEX Lite) Algorithm

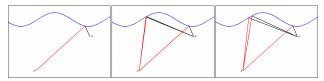
- The algorithm supports unsteady source, receiver, and sea surface motion (with some caveats, restrictions)
- The essence of the algorithm is to construct a table of values of $f(t_i) = t_i + \tau(t_i)$, by introducing first order corrections that account for the sea surface, source and receiver motion



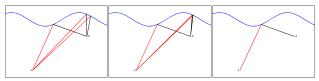
- For surface height given by $h(\vec{x}, t)$, the (first order) change in the path length is given by the expression $\Delta(t) \approx h(\vec{x}, t) \cos(\theta)$
- Step along ray, correcting $\tau(t)$ by $2\frac{\Delta(t)}{c}$ at each surface interaction

Practical Algorithms for Modeling Time-Varying Environments The VirTEX for Sea Surface Motion (VirTEX Lite) Algorithm - Continued

- Provides good agreement for cross-swell geometry
- The algorithm can breakdown in very high sea states
- Can't address situations where eigenray(s) appear and disappear



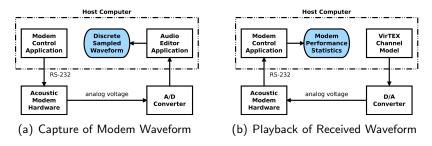
(a) Eigenrays appearing as time progresses



(b) Eigenrays disappearing as time progresses

• Generally not an issue unless source and receiver very near surface

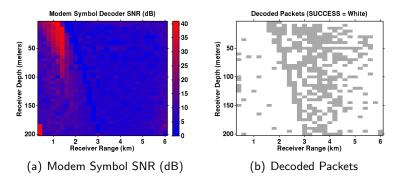
- HIL procedure for testing hardware (black box) acoustic modems
- Transducer is replaced by A/D converter (a)
- Hydrophone is replaced by D/A converter (b)
- Environment is replaced by VirTEX channel model



Applications to Acoustic Communications

Modem Sensitivity to Source, Receiver Position using VirTEX for Platform Motion

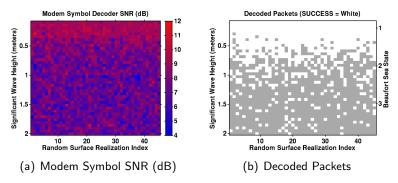
- Center frequency of 10 kHz
- Water depth of 500 m, reflective bottom
- Grid of receiver positions, moving 1.5 m/sec towards source
- Source is fixed at depth of 50 m



Applications to Acoustic Communications

Modem Sensitivity to Significant Wave Height using VirTEX for Sea Surface Motion

- Center frequency of 10 kHz
- Fixed source at depth of 75 m
- Fixed receiver at depth of 50 m
- Source and receiver separated by 500 m (both in strong surface duct)
- Multiple surface realizations for a range of significant wave heights
- JONSWAP sea surface spectrum, down-swell geometry



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Summary and Conclusions

- Two variants of the VirTEX algorithm were presented that have more modest computational resource requirements (in exchange for some restrictions on the forms of environmental motion)
- These algorithms are well suited to "what if" performance simulations
 - Testing signal processing algorithms for acoustic communications
 - Hardware-in-loop testing of commercial "black box" modems
 - Pre-deployment or pre-experiment simulations
- Acoustic modem performance is more than just transmission loss!
- Available in the next release of BELLHOP / Acoustics Toolbox
- http://oalib.hlsresearch.com/Rays/index.html